

Rotary-wing MAV Modeling & Control for indoor scenarios

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Abstract— This paper is about modeling and control of Miniature Aerial Vehicles –MAVs for indoor scenarios, specially using, micro coaxial and quadrotor systems. Mathematical models for simulation and control are introduced and subsequently applied to the commercial aircraft: the *DraganFlyer* quadrotor and the *Micro-Mosquito* coaxial flying vehicle. The MAVs have been hardware-modified in order to perform experimental autonomous flight. A novel approach for control based on Hybrid Backstepping and the Frenet-Serret theory is used for attitude stabilization (Backstepping+FST), introducing a desired attitude angle acceleration function dependent on aircraft velocity. Results of autonomous hovering and tracking are presented based on the scheme we propose for control and attitude stabilization when MAV is maneuvering at moderate speeds.

I. INTRODUCTION

Recent progress in sensor technology, data processing, and integrated actuators has made the development of Micro Aerial Vehicles –MAVs fully possible [1]-[3]. Depending on the flying principle and the propulsion mode, MAV can be classified into multiple categories: fixed, flapping, morphing and rotary wings are the most common mechanisms developed [4]-[6]. As usual, the real “*Micro*” mechanisms (at few centimeter-scale) have a span less than 15cm with a total weight less than 50 grams, and equipped with MEMS sensors and piezoelectric actuators [7], [8].

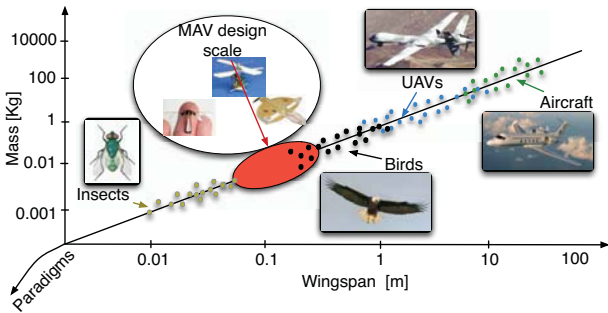


Fig. 1. Aerial Vehicles design-scale.

Depending of the size of the MAV (see Fig. 1), researchers focus on different phenomena and new paradigms and challenges related to mechanical design, electronic miniaturization [9], and new techniques for gaining more level of autonomy, which also depends on the MAV flying principle. In this sense we can observe that MAVs can be categorized in two categories: 1)-*Micro* or 2)-*Miniature* flying vehicles. In the first category, scientist focus on researching how to approach from biologically

inspired –*at-scale*– robot insects [4],[7], in which the deal is related to understand flying aerodynamics (at extremely low Reynolds numbers), and also developing/integrating electronics at that scale of design. However MAVs of the size of a small bird or even an insect are not still capable of autonomy or even 6-DoF flight, whereas the second category provides the ideal platform (due to more payload capacity and size) for testing methodologies to achieve full autonomous navigation [10],[11]. Despite nowadays the design of those *mini* aerial robots is widely extended, the full control is still a challenging goal.

In this sense, the aim of this paper is to introduce a novel control methodology named: *Backstepping+FST* to achieve reliable indoor autonomous navigation when MAV maneuvers at high speeds (up to 2m/s). Simulation and experimental testing are conducted on Vertical Take-off and Landing –VTOL systems (*like rotary-wing vehicles*) because of their unquestionable advantage compared to other concepts in terms of the ability for vertical and stationary flight, but really challenging in relation to control.

II. PROBLEM APPROACH

In terms of control, the *attitude control* of a MAV is crucial [12]. It provides the required stabilization to perform aggressive maneuvering and reliable navigation maintaining 3D orientation. Classical control (e.g. PID) applied to attitude stabilization has being used for awhile [13], however, due to its design, rotary-wing MAVs are unable to move in an uncoupled way, and as a result of this under-actuation, standard control techniques do not work well on these crafts. On the other hand, most works [14]-[17] whether use non-linear control techniques to improve on the autonomous flight, but despite the substantial interest of studying dynamics nonlinearities, and design methodologies, little attention has been paid to improve on the attitude tracking based on the velocity and acceleration of the aircraft during flight.

From a modeling perspective, both rotary-wing: the *DraganFlyer* and the coaxial *Micro-Mosquito* (see Fig. 2) have highly coupled dynamics: a change in the speed of one rotor results in motion in at least 2-DoF. For example (in the case of the *DraganFlyer*), reducing the speed of the right rotor will cause the craft to roll to the right due to the imbalance between left and right lift forces. In addition, its small size, highly coupled dynamics, low air drag on the fuselage and high air drag on the rotors, pose significant challenges in the control of this MAV.

On the other hand, coaxial structure provides enhancements related to stability and controllability due to it uses two contra-rotating rotors to compensate the torque that they apply to the fuselage when rotating. In addition a tail rotor provides to the MAV with pitch control. Nonetheless, its payload capacity (25 grams) constrains the MAV to address powerful sensing capabilities, which consequently require reinforcing the control approach.

From this analysis it becomes clear that reliable attitude stabilization is required to achieve the desired level of performance during flying. To improve on the attitude control under these characteristics, this work focuses on applying a hybrid Backstepping nonlinear control technique and the Frenet-Serret Theory–FST [18] (Backstepping+FST) that includes estimation of the desired angular acceleration as a function of the aircraft velocity, improving MAV maneuvering in presence of abrupt angular rate changes.

III. MAV SYSTEM MODELING

This section deals with the description of the fundamental concepts related to the rigid body dynamics modeling, presenting the Equations of Motion –EoM using the spatial operator algebra [19] applied to: *The DraganFlyer* [20], and the *Micro-Mosquito* [21].

A. System Description

The DraganFlyer is a radio-controlled four-rotor aerial vehicle with four channels of input to control the motion of the MAV. Varying the speed of the four rotors the motion of DraganFlyer can be controlled (propellers (1,3) and (2,4) turn in opposite directions, see Fig. 2a).

On the other hand, the Micro-Mosquito in Fig. 2b is a coaxial mechanism that flies up, down, forward, reverse, turn left and right with 3 channel digital proportional control. In the coaxial configuration, one propeller is located above the other with a common shaft.

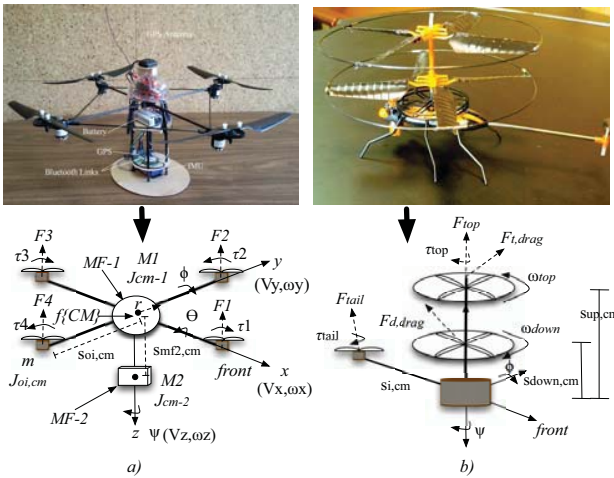


Fig. 2. MAV System Description for Modeling.

The rotors turn in opposite directions, which removes the need for a tail rotor (for torque compensation purposes), and

makes the helicopter a lot more compact. Typical coaxial MAVs use the residual torque due to angular speed difference between the two rotors to rotate the helicopter vertically, left or right. Increasing or decreasing the angular speed of the rotors simultaneously permits climbing and descending.

B. Dynamics Equations of Motion

Assuming from Fig. 3b that O_i and CM are two points located on the rigid body, and $s_{oi,cm} \in \mathbb{R}^3$ is the vector that joins the extreme border O_i with the rigid body's center of mass, the translational and angular velocities (v, ω) and forces (f, τ) respectively at any point on a body in \mathbb{R}^3 are related as shown in (1). In terms of spatial algebra, the physical quantities are represented as 6x1 column vectors, in which Euler parameterization is used for kinematics transformation. Equation 1 shows the DraganFlyer model:

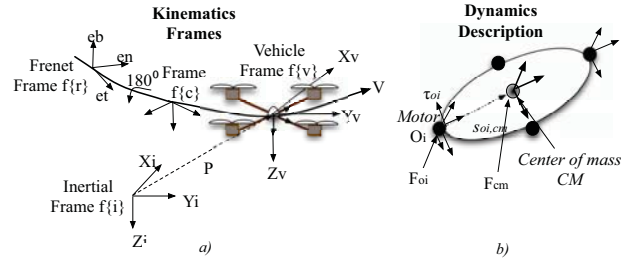


Fig. 3. MAV System Description for Modeling.

$$\begin{aligned} \dot{V}_{cm} &= \begin{bmatrix} \dot{\omega}_{cm} \\ \dot{v}_{cm} \end{bmatrix} = I_{cm,T}^{-1} [F_{cm,T} - \dot{I}_{cm,T} V_{cm}] \\ &= \begin{bmatrix} J_{cm,T} - \tilde{s}_{oi,cm} m_T \tilde{s}_{oi,cm} & m_T \tilde{s}_{oi,cm} \\ -m_T \tilde{s}_{oi,cm} & m_T U \end{bmatrix}^{-1} \begin{bmatrix} \tau_{cm,T} - \tilde{\omega}_{cm} J_{cm,T} \tilde{\omega}_{cm} \\ f_{cm,T} \end{bmatrix} \end{aligned} \quad (1)$$

The term $J_{cm,T} \in \mathbb{R}^{3 \times 3}$ in (2) indicates the total inertia of the vehicle due to rotors and electronics with total mass m_T :

$$J_{cm,T} = \frac{2}{5} M_1 r^2 + M_2 \left(\frac{a^2 + b^2}{12} + s_{mf2,cm}^2 \right) + m (r_m^2 + s_{oi,cm}^2) \quad (2)$$

For the DraganFlyer, spherical-shape has been adopted from main electronics with mass M_1 and radius r , whereas rectangular with mass M_2 and cylindrical (m, r_m) shapes for second electronics (battery + IMU) and the 4-rotors respectively. The terms (a, b) refer to the lengths of the rectangular shape assumed for second electronics (see Fig.2a).

$$\dot{V}_{cm} = \begin{bmatrix} J_{cm,T} - \tilde{s}_{oi,cm} m \tilde{s}_{oi,cm} & m \tilde{s}_{oi,cm} \\ -m \tilde{s}_{oi,cm} & m U \end{bmatrix}^{-1} \left(\begin{bmatrix} \tau_{cm,T} \\ f_{cm,T} \end{bmatrix} - \begin{bmatrix} \xi_T \\ 0 \end{bmatrix} \right) \quad (3)$$

On the other hand, the term $\tilde{s}_{oi,cm} \in \mathbb{R}^{3 \times 3}$ is the skew symmetric matrix corresponding to the vector cross product operator of $s_{oi,cm}$ (see Fig. 3 for operators description), and finally $U \in \mathbb{R}^{3 \times 3}$ refers to the identity operator. In the same way, (4) shows the Micro-mosquito dynamics model, being the velocity-dependent force term ξ_T :

$$\xi_T = \tilde{s}_{top,cm}(\tilde{\omega}_{top} J_{cm,T} \tilde{\omega}_{top}) + \tilde{s}_{down,cm}(\tilde{\omega}_{down} J_{cm,T} \tilde{\omega}_{down}) + \tilde{s}_{oi,cm}(\tilde{\omega}_{tail} J_{cm,T} \tilde{\omega}_{tail}) \quad (4)$$

Where the total inertia term $J_{cm,T}$ corresponds:

$$J_{cm,T} = \frac{R_p^2}{4} + \frac{e_p^2}{12} (s_{up,cm}^2 + s_{down,cm}^2) + m \frac{a^2 + b^2}{12} \quad (5)$$

The parameters R_p and e_p refer to the radius and thickness of the disk-shape formed by propeller rotation. Terms (a,b) to the lengths of a rectangle-box shape assumed for electronics onboard. In addition the Table-I shows the electronics component description of both MAV.

TABLE I
MAV ELECTRONICS COMPONENT DESCRIPTION

DraganFlyer	Micro-Mosquito
Width: 0.63m	Length: 18.5 cm
Rotor span: 0.35m	Control: 3 ch. digital FM
Main battery: 92 grams	Motors: 7 mm coreless + 4 mm for tail.
IMU: 40 grams	Battery: 160 mAh li-po
Bluetooth card-1: 10 grams	Flight time: about 10 min
GPS: 17 grams	Rotor span: 16cm
Antenna: 45 grams	Height: 8cm
Voltage Converter: 25 grams	
Bluetooth card-2: 7 grams	
Mainframe: 25 gram	
Total weight: 686 grams	Total weight: 20 grams

IV. AUTONOMOUS FLIGHT

For achieving full autonomous flight, two main modules compose the architecture for modeling and control: *The System Modeling* (previously introduced in section-III), and *The System control* (see Fig. 4). In terms of control, mapping the commands from control space to force space requires a model of the forces and their interactions. In the case of the DraganFlyer, each motor produces a force (F) and torque (τ). For the rotational force-components, the rolling torque is produced by the forces of the right and left motors: τ_2 and τ_4 , similarly the pitching torque is produced by the forces of the front and back actuators: τ_3 and τ_1 . For the Micro-Mosquito pitching torque is proportional to tail lift force and yawing torque is proportional to the difference in rotation of main propellers.

During the development of this project we explored several control methodologies from theoretical development

to final experiments. As a first attempt, we tested on DraganFlyer a PID controller based on a simplified

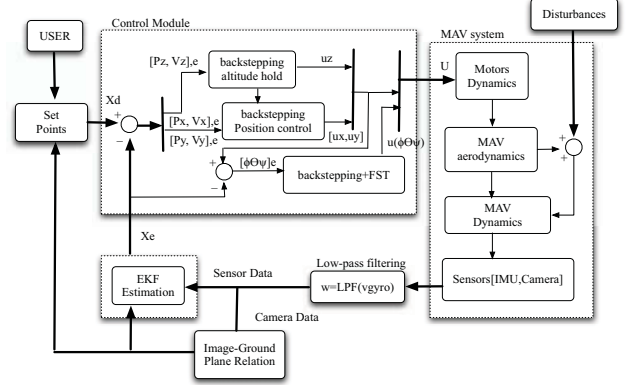


Fig. 4. Architecture for MAV autonomous flight.

model, however strong disturbances were poorly rejected. In the second attempt we reinforced the control using backstepping technique. This time, simulation and experimental results confirmed improvements in relation to disturbance rejection.

The backstepping technique has been used for some time for controlling quadrotors [10]. Improvements have been introduced thanks to combine integral action within the control law (integral-backstepping), which consequently asymptotic stability is guaranteed as well as steady state errors cancelation due to integral action. Nonetheless, poor analysis has been conducted on specifically improving attitude control, while the aircraft is maneuvering at moderate speeds and performing aggressive changes in orientation. To improve on this, we have adopted the Frenet-Serret formulation used in vector calculus to describe the kinematic properties of the aircraft that moves along a continuous and differentiable curve in the Euclidian space. Consequently, improvements on attitude stabilization using integral-backstepping+FST as a function of a desired aircraft acceleration command are achieved. Next section explains this issue in detail.

A. System Control

The complete system control is composed by a cascade-connection of altitude, position and attitude controllers (see Fig. 4). Attitude control is the heart of the control system that maintains the MAV stable and oriented towards the desired direction. This section shows *roll*-control derivation based on hybrid backstepping and the Frenet-Serret equations previously introduced. Note that for both *pitch* and *yaw*-control the same methodology is used. Based on the dynamics model from (1), the first step is considering the *roll* tracking error of the DraganFlyer e_1 and its derivative with respect to time.

$$\begin{aligned} e_1 &= \phi^d - \phi \\ \dot{e}_1 &= \dot{\phi}^d - \omega_x \end{aligned} \quad (6)$$

A Lyapunov function (positive definite) is used for stabilizing the tracking error e_1 , based on a virtual control law for setting the desired behavior of the angular speed ω_x :

$$\begin{aligned} V(e_1) &= \frac{e_1^2}{2} \\ \dot{V}(e_1) &= e_1(\dot{\phi}^d - \omega_x) \end{aligned} \quad (7)$$

The virtual control law for stabilizing the angular tracking error e_2 is then defined as:

$$\begin{aligned} e_2 &= \omega_x^d - \omega_x \\ \omega_x^d &= c_1 e_1 + \dot{\phi}^d + \lambda_1 \int e_1 \end{aligned} \quad (8)$$

Replacing the ω_x^d term in (8), and deriving e_2 with respect to time:

$$\begin{aligned} e_2 &= c_1 e_1 + \dot{\phi}^d + \lambda_1 \int e_1 - \omega_x \\ \dot{e}_2 &= c_1(\dot{\phi}^d - \omega_x) + \ddot{\phi}^d + \lambda_1 e_1 - \ddot{\phi} \end{aligned} \quad (9)$$

Now replacing ω_x from (8) into \dot{e}_1 in (6), and then replacing \dot{e}_1 into \dot{e}_2 in (9):

$$\begin{aligned} \dot{e}_1 &= -c_1 e_1 - \lambda_1 \int e_1 + e_2 \\ \dot{e}_2 &= c_1(-c_1 e_1 - \lambda_1 \int e_1 + e_2) + \ddot{\phi}^d + \lambda_1 e_1 - \ddot{\phi} \end{aligned} \quad (10)$$

Extracting from (1) the dynamics terms corresponding to angular acceleration $\ddot{\phi}$ of the DraganFlyer, and replacing them into (10):

$$\begin{aligned} \dot{e}_2 &= c_1(-c_1 e_1 - \lambda_1 \int e_1 + e_2) + \ddot{\phi}^d + \\ &\quad \lambda_1 e_1 - J_{x-cm,T}^{-1} [\dot{\theta} \psi (J_{y-cm,T} - J_{z-cm,T}) + \tau_\phi] \end{aligned} \quad (11)$$

Solving (11) for τ_ϕ which is the control law for achieving *roll* stabilization, and defining the desirable dynamics for the angular speed tracking error as $\dot{e}_2 = -e_1 - c_2 e_2$:

$$\begin{aligned} \tau_\phi &= J_{x-cm,T} \Omega + \xi \\ \Omega &= e_1(c_1^2 - 1 - \lambda_1) - e_2(c_1 + c_2) + c_1 \lambda_1 \int e_1 - \ddot{\phi}^d \\ \xi &= \dot{\theta} \psi (J_{y-cm,T} - J_{z-cm,T}) \end{aligned} \quad (12)$$

Finally, the term $\ddot{\phi}^d$ in (12) is replaced by the desired angular acceleration command to be obtained with the Ferret theory. To understand how to obtain this term, refer to Fig. 3a in which the different frames used to operate the EoM were introduced. The Vehicle-frame $f\{v\}$ and the

Inertial-frame $F\{i\}$ that are related with each other using Euler parameterization, and two additional frames called the Frenet-frame $f\{r\}$ and the rotated Frenet-frame $f\{c\}$ which are composed by three unit vector so-called the tangent (e_t), normal (e_n), and binormal (e_b), that move along the curve or desired trajectory. Imagine that an observer moves along the curve in time, using the attached frame at each point as its coordinate system. The Frenet-Serret formulas mean that this coordinate system is constantly rotating as an observer moves along the curve; hence, this coordinate system is always non-inertial. So, the position and the magnitude of the velocity vector at any point of the trajectory are given by:

$$V = \|\dot{P}\| = \sqrt{\dot{P}_x^2 + \dot{P}_y^2 + \dot{P}_z^2} \quad (13)$$

To every point of the curve we can associate an orthonormal triad of vectors namely the tangent, the normal and the bio-normal (see Fig. 3a). Properly arranging these vectors, we obtain a description of the curve orientation. The corresponding reference frame is the Frenet-Serret $f\{r\}$ one.

$$e_t = \frac{\dot{P}}{V}, \quad e_b = \frac{(\dot{P} \times \ddot{P})}{\|\dot{P} \times \ddot{P}\|}, \quad e_n = e_b \times e_t \quad (14)$$

As far as the reference orientation $[\phi_R, \theta_R, \psi_R]^T$ of the body-fixed frame $f\{v\}$ with respect to the inertial $f\{i\}$ frame is concerned, due to the dynamics, $f\{v\}$ does not coincide with the $f\{c\}$ frame. To eventually coincide with the reference desired frame $f\{R\}$ that provides the orientation consistent with the aircraft dynamics, the rotation of the $f\{v\}$ frame from $f\{c\}$ to $f\{R\}$ can be expressed using customary aeronautical notation by considering the sideslip angle β , and the angle of attack α :

$$\begin{aligned} \beta &= \sin^{-1} \left(\frac{\dot{P}_y}{V} \right), \quad \alpha = \tan^{-1} \left(\frac{\dot{P}_z}{\dot{P}_x} \right) \\ R_{\{c\}}^{\{R\}} &= R_y^T(\alpha) R_z^T(-\beta) \\ R_{\{i\}}^{\{R\}} &= R_{\{c\}}^{\{R\}} R_{\{c\}}^{\{i\}T} \end{aligned} \quad (15)$$

Using the second derivative of $R_{\{i\}}^{\{R\}}$ with respect to time, the angular acceleration references can be extracted from matrix components as:

$$\begin{aligned} \ddot{\phi}^d &= \frac{d^2}{dt^2} \left(\text{atan2} \left(R_{\{i\},23}^{\{R\}}, R_{\{i\},33}^{\{R\}} \right) \right) \\ \ddot{\theta}^d &= \frac{d^2}{dt^2} \left(\text{atan2} \left(-R_{\{i\},13}^{\{R\}}, \sqrt{\left(R_{\{i\},23}^{\{R\}} \right)^2 + \left(R_{\{i\},33}^{\{R\}} \right)^2} \right) \right) \\ \ddot{\psi}^d &= \frac{d^2}{dt^2} \left(\text{atan2} \left(R_{\{i\},12}^{\{R\}}, R_{\{i\},11}^{\{R\}} \right) \right) \end{aligned} \quad (16)$$

Replacing $\ddot{\phi}^d$ from (16) into (12), the Backstepping+FST

control is presented. Next section presents experimental and simulation results conducted on both MAV platforms.

V. RESULTS

In order to validate that our assumption of improving attitude stabilization within the Backstepping+FST is indeed correct, Fig. 5 and 6 show the experimental results for the first test performed using the DraganFlyer MAV. Control parameters used in this experiment are: for *roll*: $[c_1, c_2, \lambda_1] = [5.5, 0.5, 0.01]$, *pitch*: $[c_3, c_4, \lambda_2] = [10, 2, 0.01]$, *yaw*: $[c_5, c_6, \lambda_3] = [2, 1.5, 0.005]$.

Note in Fig. 6 the PID controller proved to be well adapted to the MAV when flying near to hover. For this kind of test (hovering control), there are not huge differences of using the backstepping+FST control against single backstepping or either PID controllers. Note that just a slight difference in relation to amplitude and time oscillation is improved with the backstepping+FST. The reason is that this controller has been designed to improve on the attitude stabilization when aircraft is maneuvering at moderate speed. To take advantage of the backstepping+FST, the trajectory of the aircraft must be smooth enough (e.g. three-times differentiable with respect to time) in order to achieve the desired values of attitude angles based on the references.

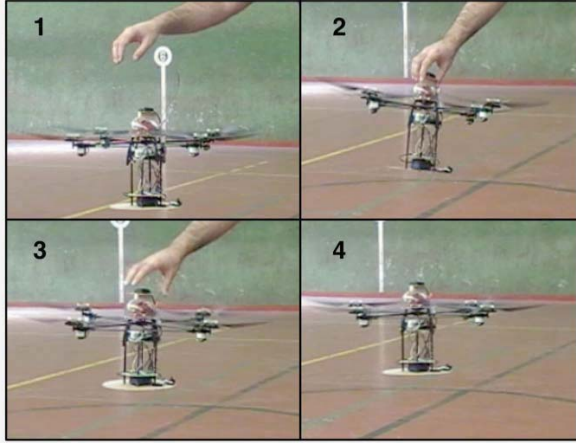


Fig. 5. Strong external disturbances addressed during experiment in Fig. 6.

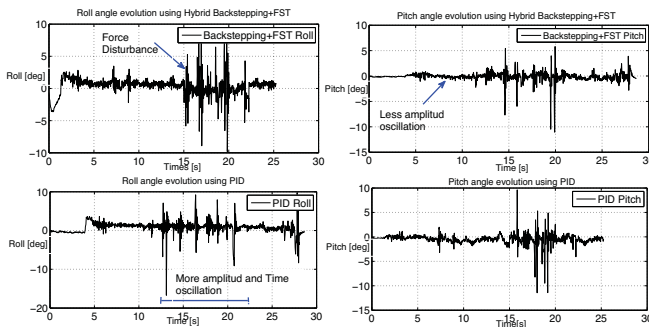


Fig. 6. Attitude control: Comparison between backstepping+FST control against PID controller while maintaining aircraft attitude angles to zero.

To achieve full indoor autonomous navigation (altitude

and position), a camera must be placed on the MAV. For instance, the DraganFlyer platform has just been hardware-modified by addressing IMU and GPS for outdoor navigation. Our final goal on this project is to address the camera onboard for both DraganFlyer and Micro-Mosquito in order to perform tracking tasks based on vision.

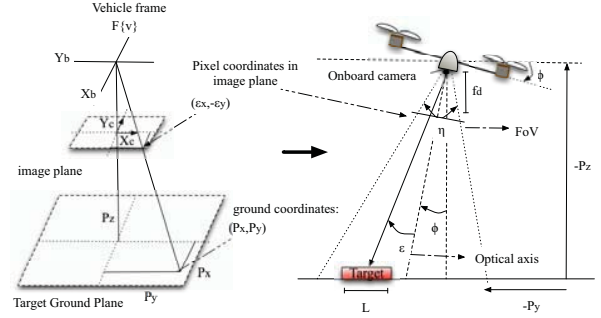


Fig. 7. Camera model for indoor navigation

The control objective is to maintain the vehicle in a constant altitude (P_z) while tracing the horizontal trajectory defined by the target on ground (see Fig. 7). For altitude and position control (same backstepping approach used in (11) is adopted), and camera information based on relating the real size of the target (L), the size of the target projected in the image plane ε (given in pixels), the focal distance fd and the altitude to hold P_z , are used for defining the control laws.

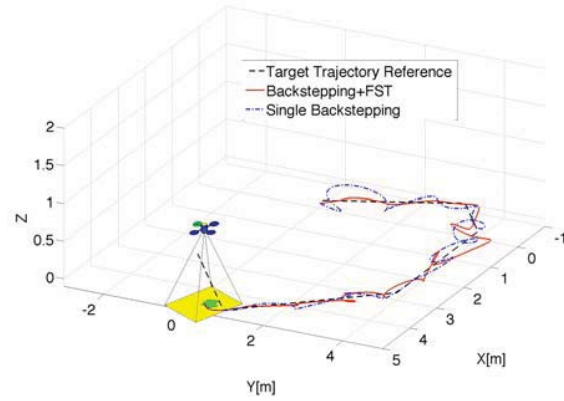


Fig. 8. DraganFlyer full navigation simulation experiment: indoor navigation based on tracking a target on ground up to speeds of 2m/s (including wind disturbances of 0.5m/s in both x-y axes).

From Fig. 8 note that target's trajectory profile performs four-aggressive orientation changes (*yaw-angle*) during tracking at linear speed of 2m/s. The DraganFlyer perfectly tracked the target maintaining the orientation given by the target at 1[m]-altitude from ground. Because of the angular acceleration estimation introduced in the Backstepping +FST, attitude stabilization based on the aircraft velocity profile improves on the tracking error (in X-Y position) of the quadrotor while tracking the target. In addition, external disturbances are poorly rejected using the single

backstepping approach against the FST inclusion.

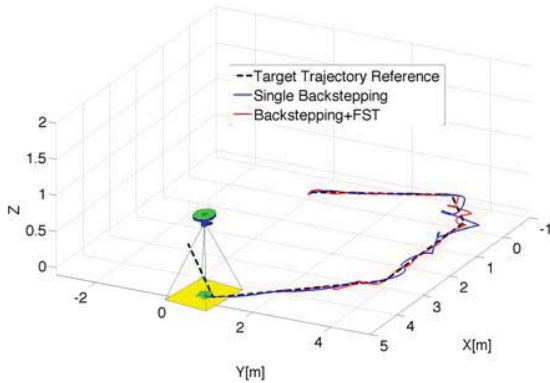


Fig. 9. Micro-Mosquito full navigation simulation experiment: indoor navigation based on tracking a target on ground up to speeds of 2m/s.

Backstepping+FST is being applied to the Micro-Mosquito MAV. As shown in Fig. 9, improvements on attitude stabilization also improves on position tracking compared to single Backstepping approach. In this case, note that the coaxial mechanism is more stable during flight compared to the quadrotor system.

VI. CONCLUSIONS

A hybrid Backstepping+FST methodology has been proposed for attitude control for MAV autonomous navigation. Experimental results performed in Fig. 5 and 6 showed how the control maintains attitude references in presence of external disturbances.

For full indoor navigation, Future work includes addressing vision capability to the DraganFlyer and the Micro-Mosquito, and finally testing position and altitude control beyond simulation. Nonetheless, results obtained in Fig. 8 and 9 are motivating. At high speed maneuvering (2m/s), the backstepping+FST's performance (in relation to error tracking) is about 3.5x times better than using the single backstepping technique (in the case of the DraganFlyer). For the Micro-Mosquito, the tracking is even more reliable thanks to the advantage related to the stabilization presented on coaxial mechanisms.

For both cases, the improvement in tracking was basically achieved by introducing a desired angular acceleration command (as a function of the maneuvering velocity) that quickly responds to abrupt angular rate change, making the attitude stabilization more reliable.

ACKNOWLEDGMENT

This work was supported by the Robotics and Cybernetics Group at Technique University of Madrid, Spain and funded under the project FRACTAL: Fleet of cooperative terrestrial and aerial robots, sponsored by the Spain Ministry of Education and Science (DPI 2006-03444) and ROBOCITY 2030 (S-0505/DPI/ 000235), <http://www.robocity2030.org/>

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